

Formation of H₂

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KEY ISSUES

- What is the H₂ formation efficiency at high dust temperatures?
- What is the rate of formation?

Predictions of models

Can it be determined from observations of PDRs?

- Excitation of newly formed molecules
 - distribution over vibration-rotation states (v, J)
 - line broadening of kinetically hot molecules?
 - do these effects leave observable signatures?

BENCHMARKING RATE

Expressed as a binary rate coefficient:

$$R = 3 \times 10^{-18} T_{\text{gas}}^{1/2} n(\text{H}) n_{\text{H}} \text{ cm}^{-3} \text{ s}^{-1}$$

thus, for example, $R = 2.121 \times 10^{-17} n(\text{H}) n_{\text{H}} \text{ cm}^{-3} \text{ s}^{-1}$ at $T_{\text{gas}} = 50 \text{ K}$. This form of the rate follows from Hollenbach, Werner, and Salpeter (1971).

EXPERIMENTS

Pirronello and collaborators have measured association of HD and H₂ on silicate (olivine) and amorphous carbon surfaces, which were designed to be good experimental analogues of interstellar dust surfaces. Because several processes are occurring in the transformation of H into H₂ on a surface

- H atoms collide with a surface
- H atoms bind to the surface and migrate around on it
- H atoms meet on the surface and associate to form H₂
- H-atom desorption may occur before association
- H₂ desorption releases the new molecule into the gas phase

it is necessary to construct a numerical model of the experiments. This consists mainly in a pair of coupled differential rate equations. Katz et al. (1999) presented such a model of the experiments and Biham et al. (1998) discussed the behavior of two limiting cases in the astrophysical context.

Cazaux & Tielens (2004) offered an alternative model that incorporates chemisorption and tunneling as well as the processes considered by Katz et al. Cazaux & Tielens conclude that the association efficiency can remain high even for warm surfaces ($T_{\text{surface}} \geq 100$ K). Cazaux & Tielens (2002) had previously applied their model to the computation of association efficiencies that can be included in the astrophysical rate.

I have taken the model of Katz et al. and integrated the formation efficiency over the standard particle-size distribution of Mathis, Rumpl, and Nordsieck in order to express the experimentally determined rate in terms of a binary rate coefficient; i.e., a form that can be compared directly with the benchmarking rate (above). Examples are shown in the following tables. Details are explained in accompanying notes.

Effective binary rate coefficients R_{eff} [$\text{cm}^3 \text{s}^{-1}$]
 Conditions of model F1: $T_{\text{gas}} = 50$ K, $T_{\text{surface}} = 20$ K, $n_{\text{H}} = 10^3 \text{ cm}^{-3}$

$n(\text{H})$	R_{eff} silicate	R_{eff} carbon
10^3	1.5E-20	7.4E-17
10^2	1.5E-21	6.6E-17
10	1.5E-22	4.9E-17
1	1.5E-23	2.6E-17

Dependence of rate on T_{surface} at $T_{\text{gas}} = 300$ K, $n(\text{H}) = 10^3$

T_{surface}	R_{eff} silicate	R_{eff} carbon
12	1.7E-16	2.1E-20*
15	3.1E-17	5.6E-17*
20	8.7E-20	1.8E-16
25	9.0E-22	5.9E-17
30	4.2E-23	3.4E-18
35	4.8E-24	9.5E-20

*Note: for these conditions, H_2 formation on the surface achieves the steady-state limit only after times of the order of 10^5 s or longer.