

# Summary I

- H<sub>2</sub> Shielding: --  $\beta(\tau)$  vs full H<sub>2</sub>,  
correction for  
sphere/slab,  $G_0/n$   
alone not whole story
- line overlap important  
or not?
- determine thin rates  
with  $\int I(\lambda)\sigma(\lambda)d\lambda$  (no fit)

# Summary II

- Line Transfer: -- Optically thick, effectively thin line has higher  $n_i$  in sphere vs slab (for same  $T$ )
  - In MC vs ALI beware convergence for  $\tau \gg 1$
  - Check levels  $n_i$  not just  $T_R$  or total  $I$

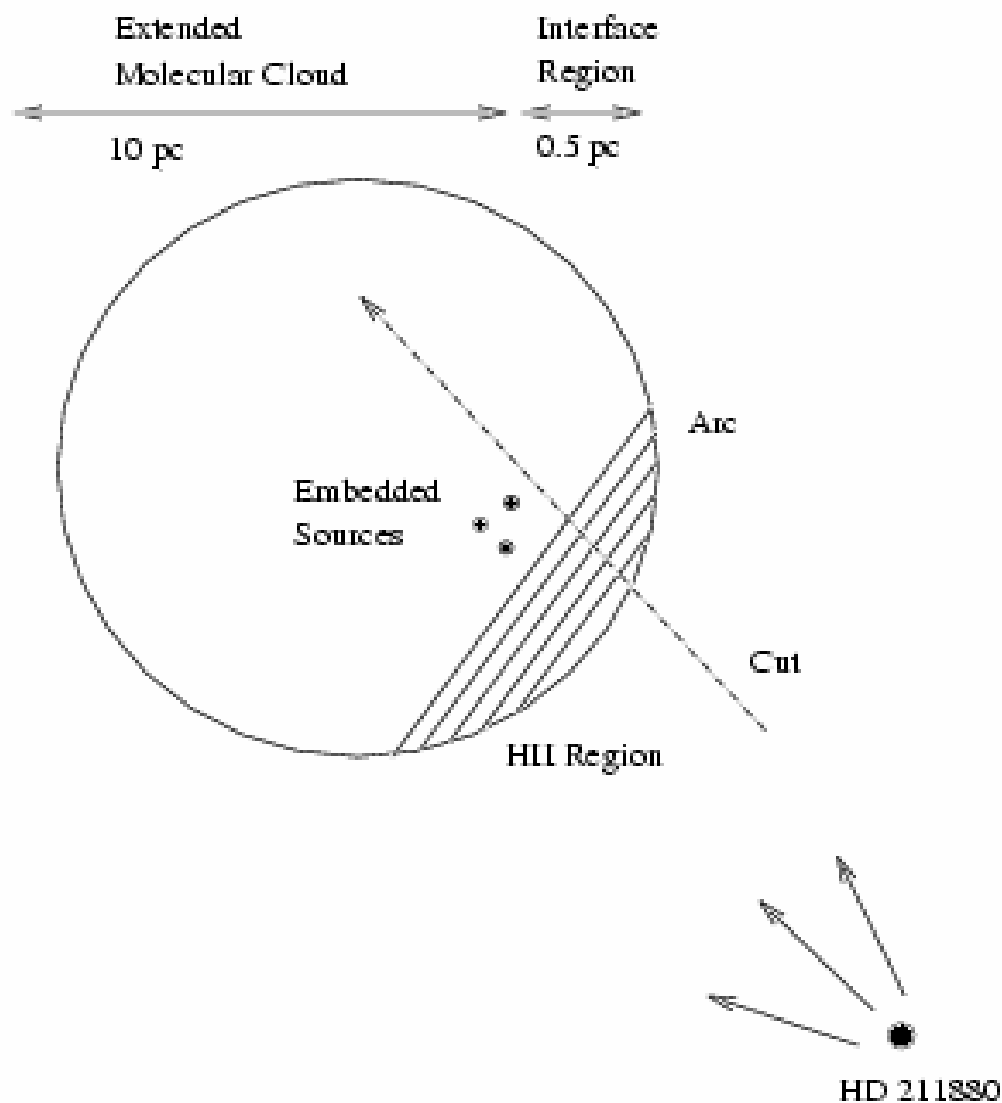
# Photon Processes in (Inhomogeneous) PDRs

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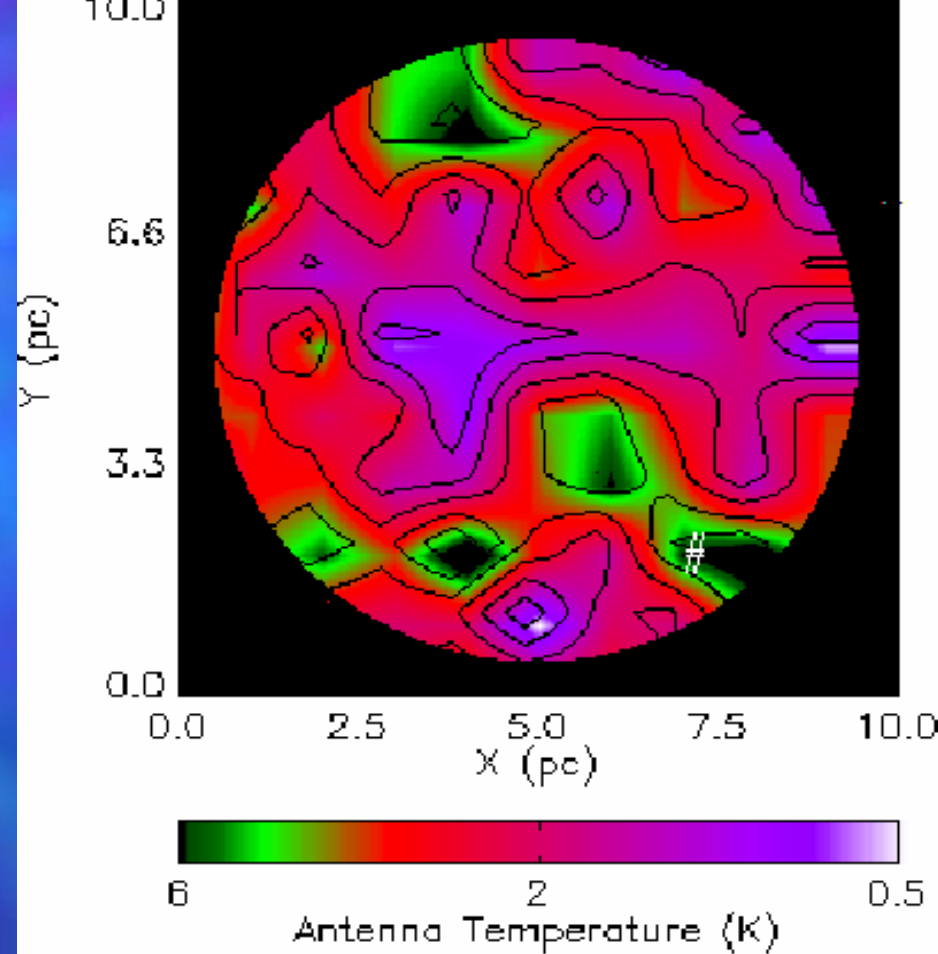
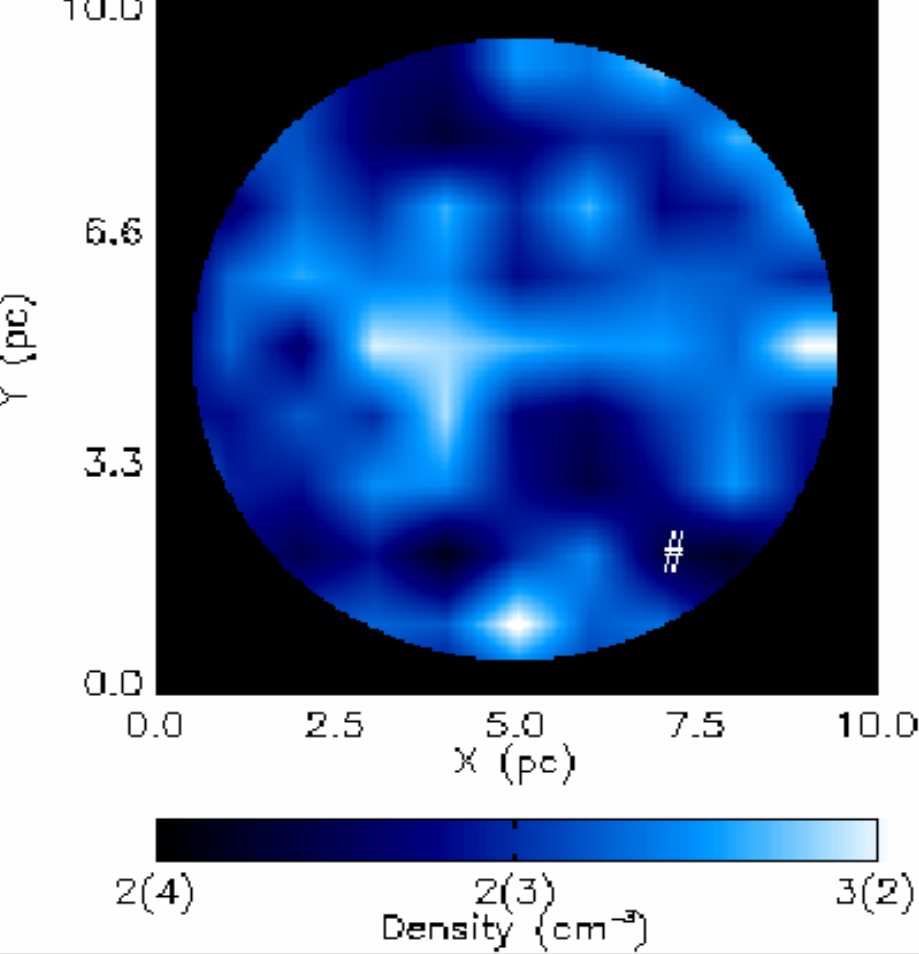
Marco Spaans (Kapteyn)

# Clumpiness

- Parameter  $k$  decreases in expression for  $R$
- For given  $N_H$  columns of  $C^+$  and  $C$  not strongly affected, but spatial extent is
- Column density of  $CO$  is boosted in dense clumps
- Back scattering of UV photons causes complicated clump illumination:  
 $\langle \cos \theta \rangle(\lambda)$  and  $\omega(\lambda)$
- Influences  $C^+ \rightarrow C \rightarrow CO$  transition

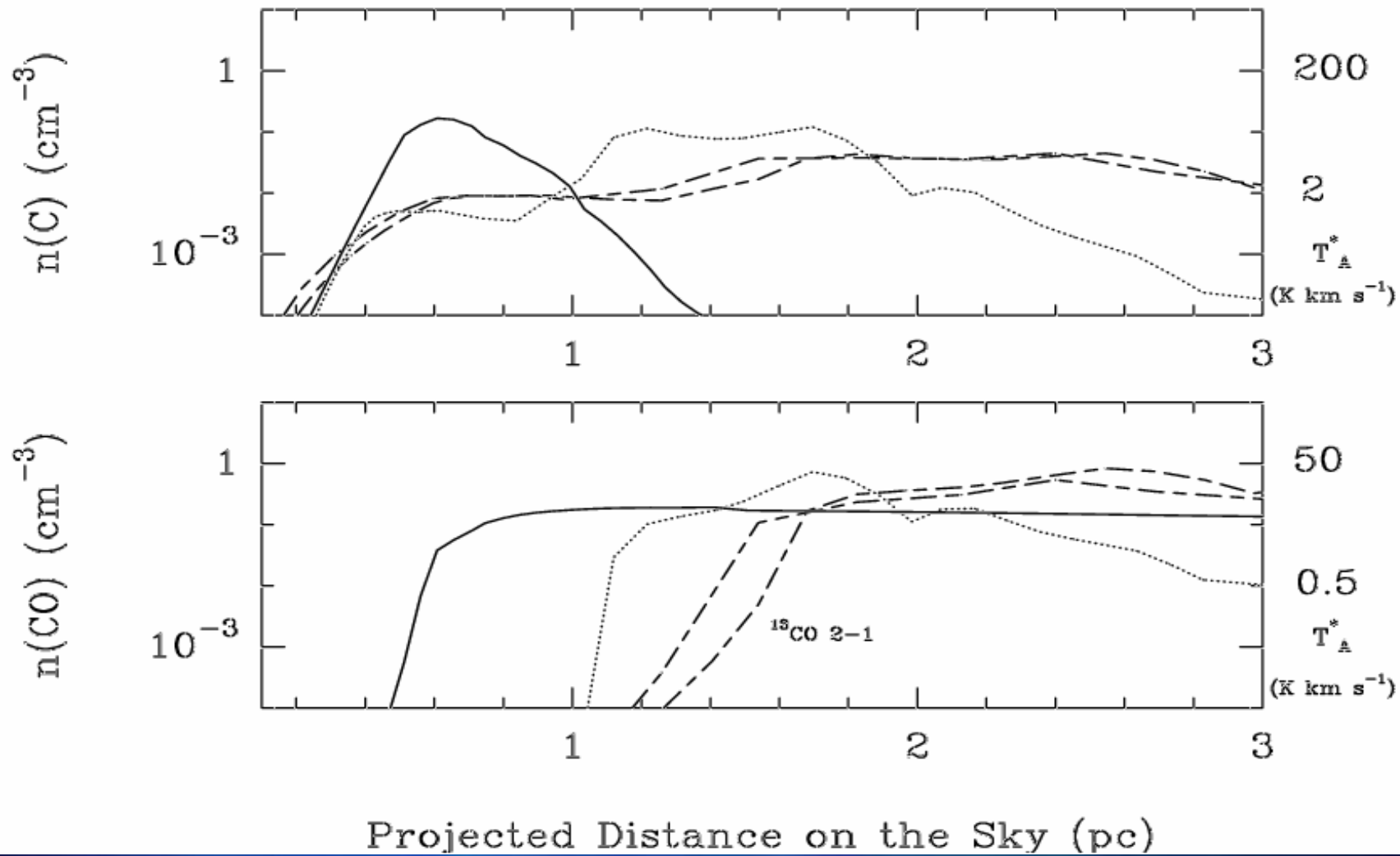


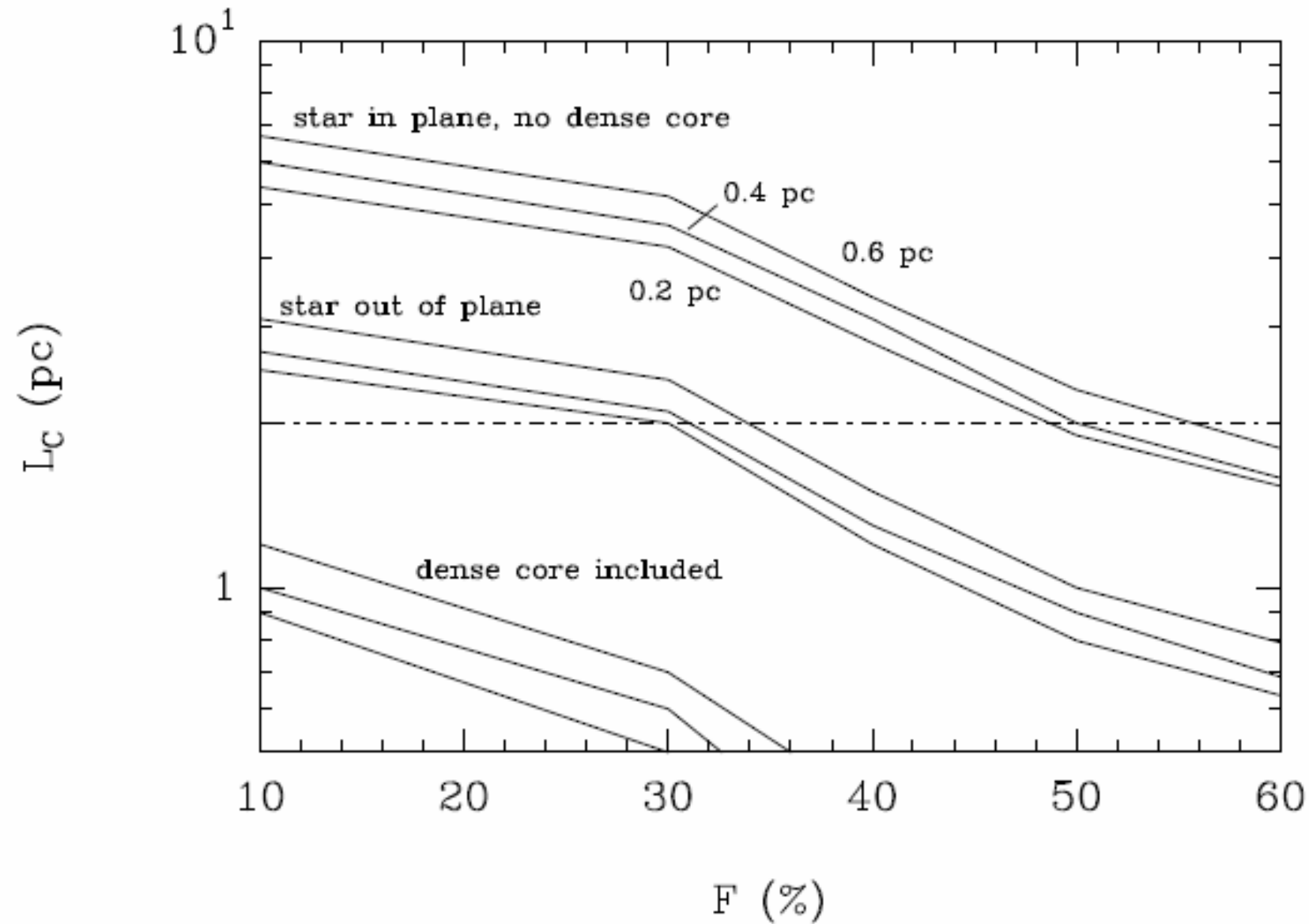
- S140, edge-on PDR
- $n = F n_c + (1 - F) n_i$
- $r = n_c / n_i$ , clump size  $l_c = 0.02$  pc
- $I_{uv} = 140$ ,  $F = 30\%$ ,  $r = 10$ ,  $n = 2(4) \text{ cm}^{-3}$



total H density

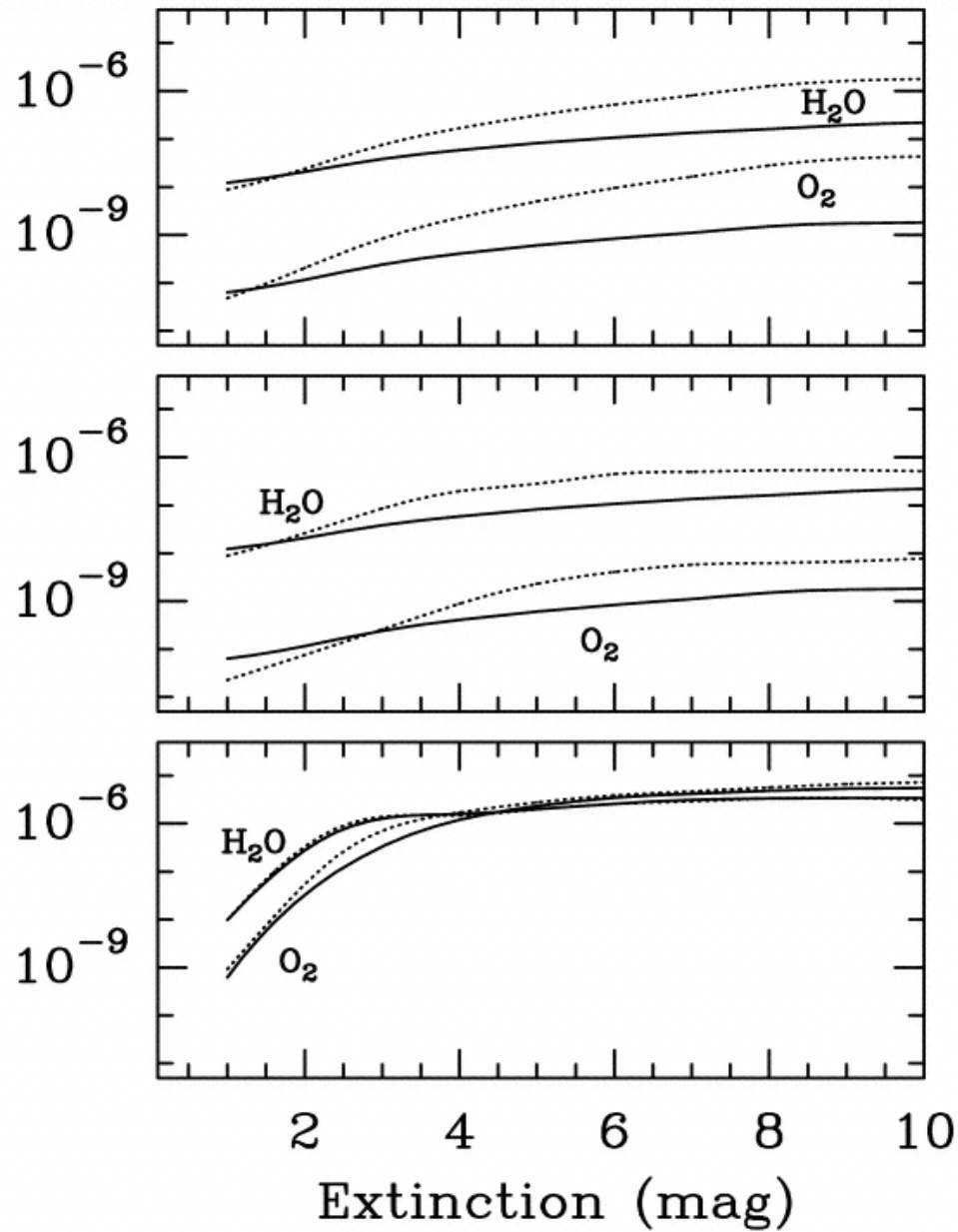
[CI] 609  $\mu\text{m}$  &  
 $^{13}\text{CO}$  2-1





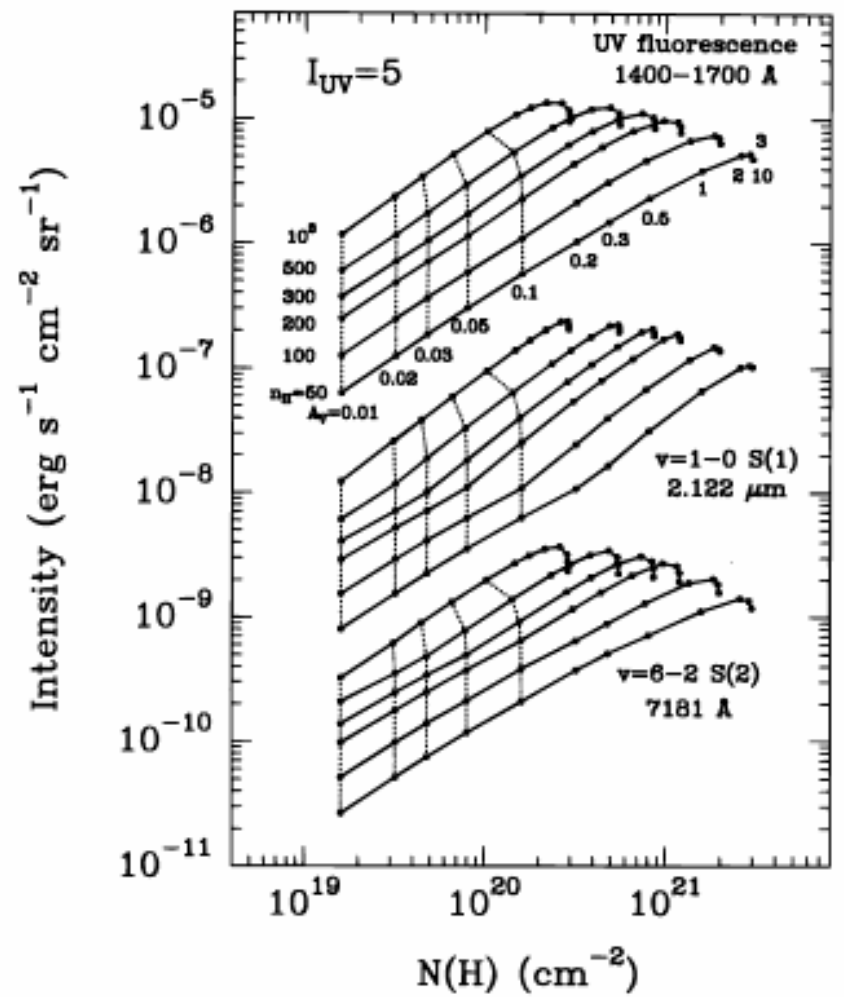
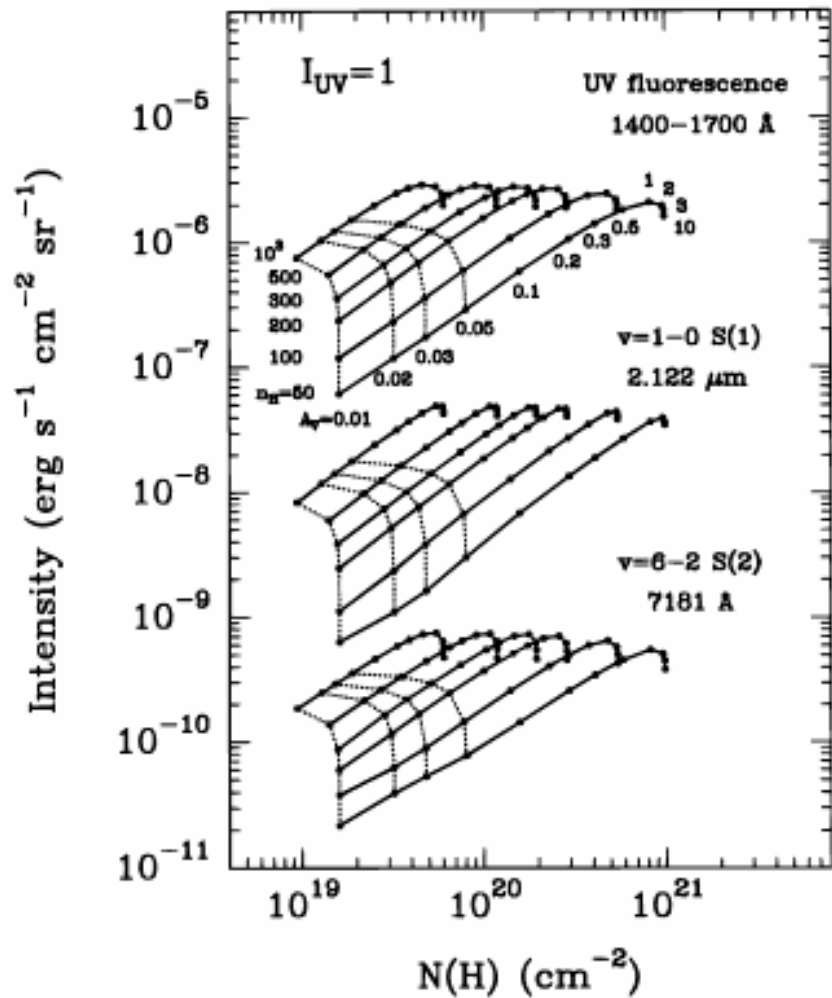


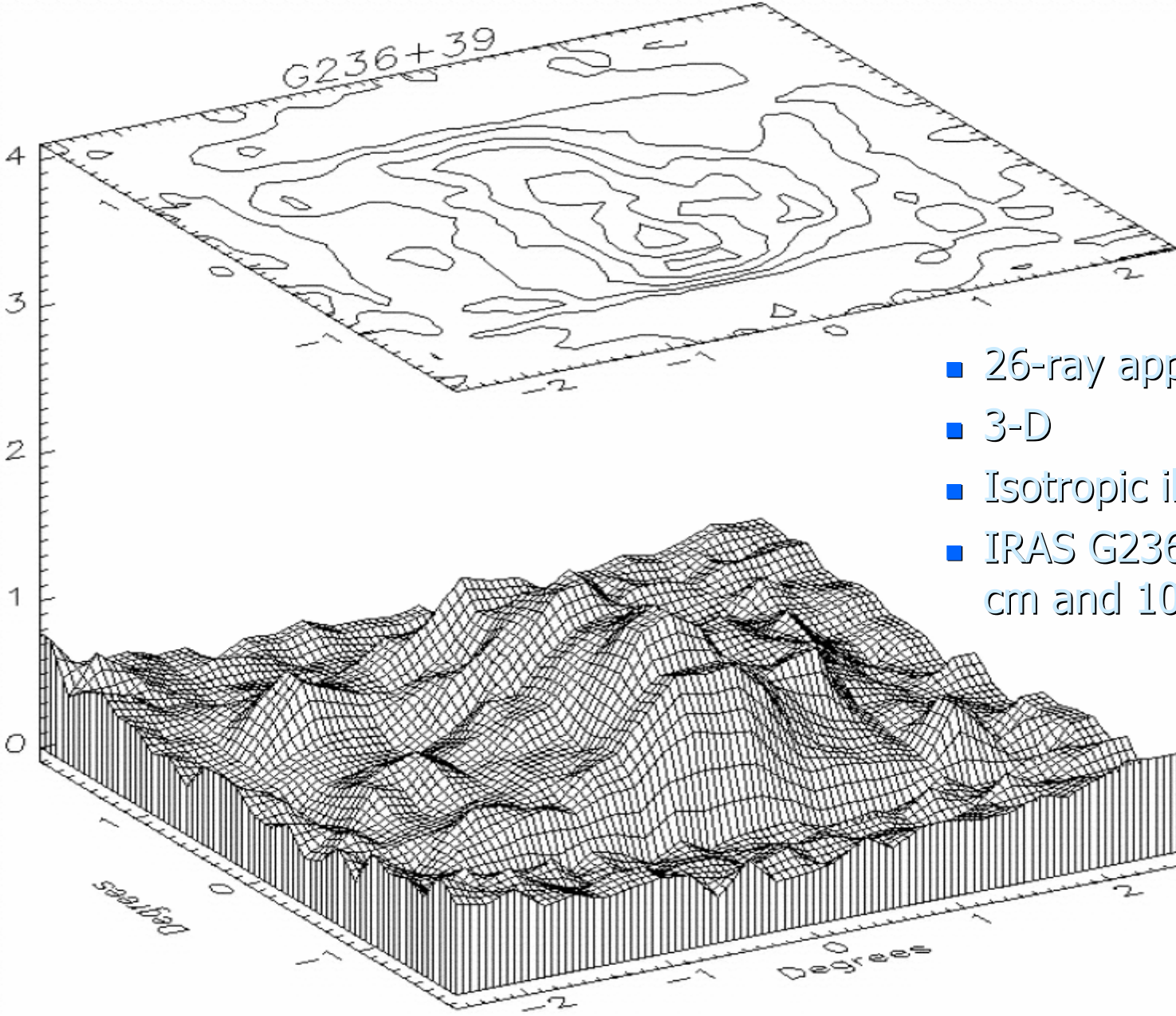
Abundance



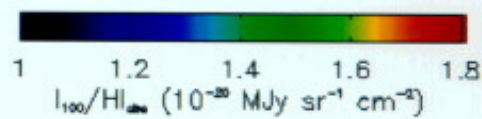
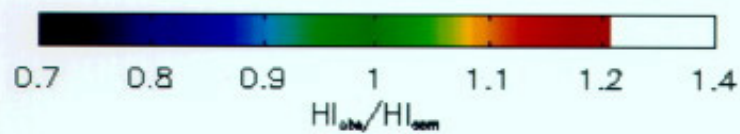
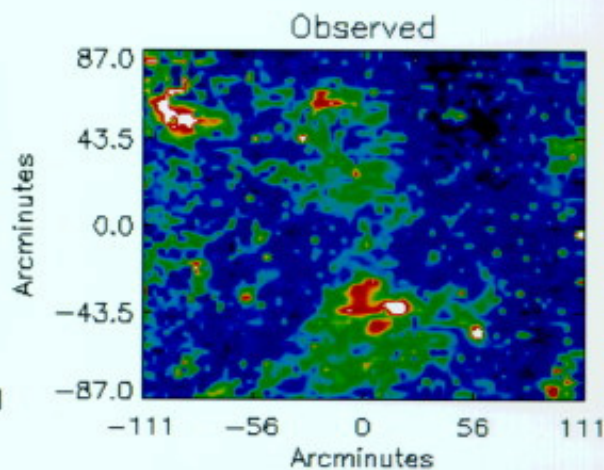
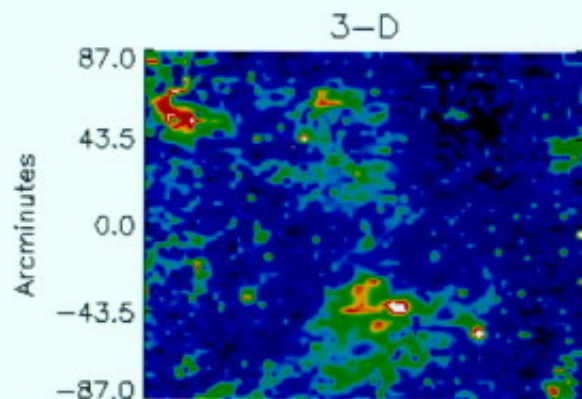
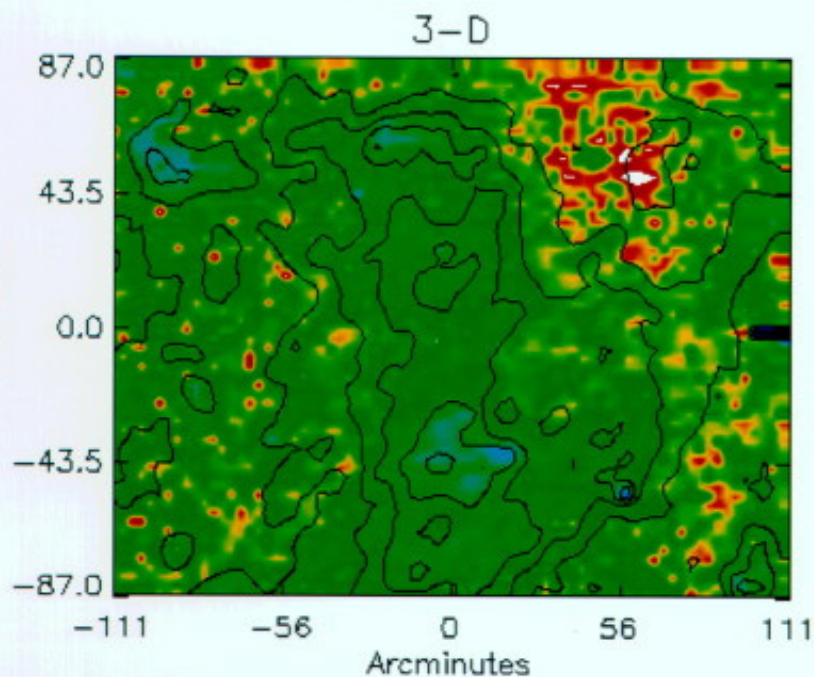
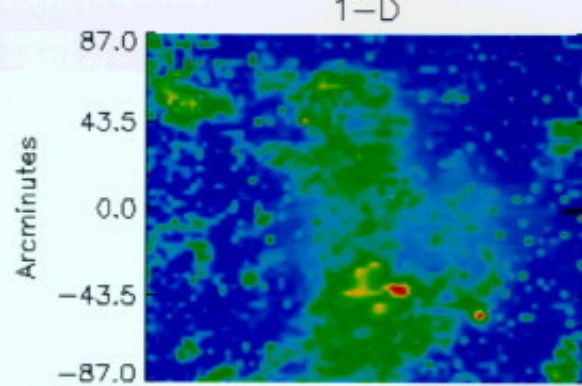
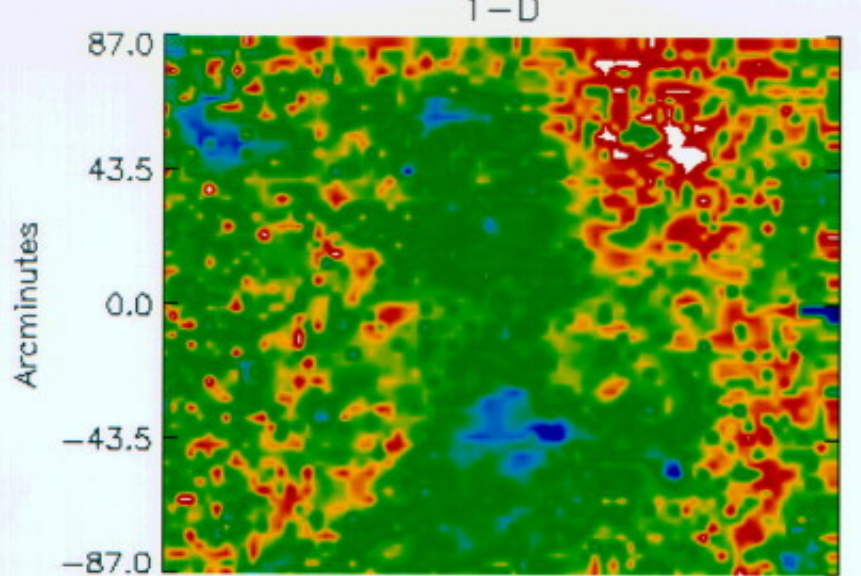
# H<sub>2</sub> emission

- Fluorescence:
  - UV – Vis – IR
  - Diagnostic for  $I_{uv}/n_H$
  - No collisional de-excitation if density less than  $10^4 \text{ cm}^{-3}$  (same for multiple pumping)
- Scaling:  $I_F/I_{uv}$  ( $Rn_H/I_{uv}, N_H$ ) and  $N_H(Rn_H/I_{uv}, A_V)$
- Also pure rotational line emission





- 26-ray approximation
- 3-D
- Isotropic illumination
- IRAS G236+39: HI 21 cm and 100  $\mu$ m dust



# Photorates with depth

- $R = R_0 e^{-k A_V}$ ;  $R_0$  strong function of  $T_{\text{eff}}$
- $k$  is a fit and  $k \sim 1-3$
- CO (absorptions into pre-dissociated states) and  $\text{H}_2$  (Lyman-Werner+cascade) self-shield;  
TH, de Jong et al.:  
$$\beta_{\text{H}_2}(\tau > 10) = \left\{ \tau^{-1} [\ln(\tau/\pi^{1/2})]^{1/2} + (b/\tau)^{1/2} \right\} \text{erfc}(\tau b/\pi v^{-2})^{1/2}$$
$$R_{\text{CO}} * [1 + a\beta_{\text{CO}}(\tau)] / (1 + a)$$
 or shielding functions van Dishoeck & Black (1988)

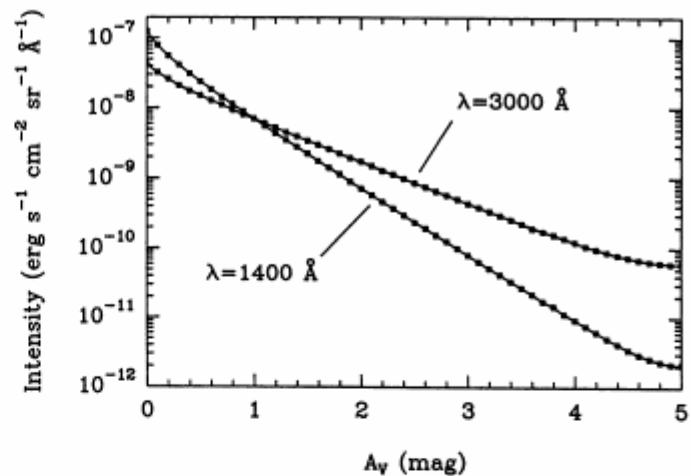
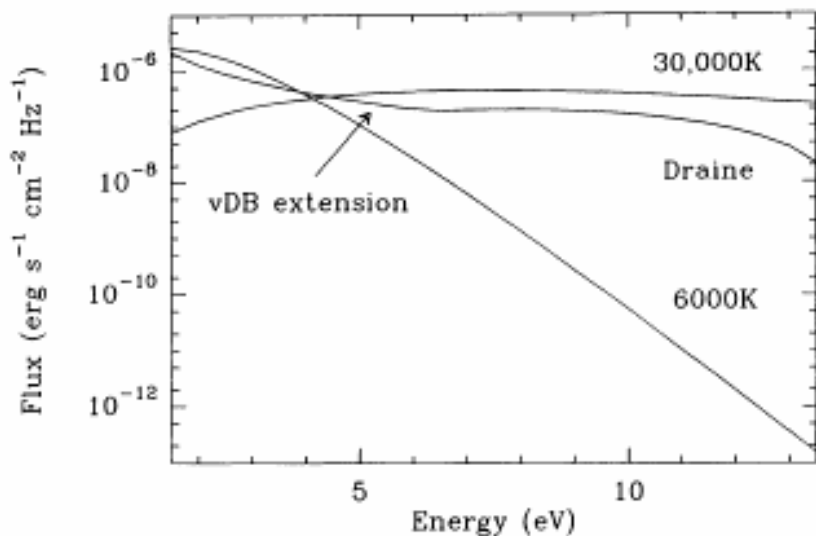
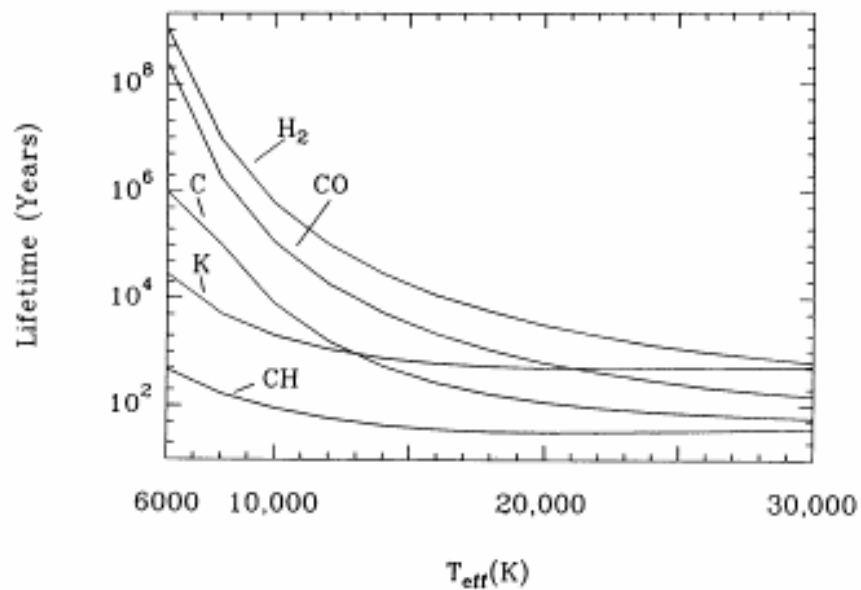


FIG. 2.—Comparison between the Draine (1978) field and the normalized 6000 and 30,000 K blackbody curves. For  $\lambda > 2000 \text{ \AA}$ , the representation of van Dishoeck & Black (1982) was used.



SHIELDING FUNCTIONS  $\Theta[N(\text{CO}), N(\text{H}_2)]^a$ 

log $N(\text{H}_2)$	log $N(\text{CO})$							
	0	13	14	15	16	17	18	19
$^{12}\text{CO}$ : Unattenuated Rate <sup>b</sup> $k_{10} = 2.039 \times 10^{-10} I_{\text{UV}} \text{ s}^{-1}$								
0.....	1.000	9.681(-1)	7.764(-1)	3.631(-1)	7.013(-2)	1.295(-2)	1.738(-3)	9.985(-5)
19.....	8.215(-1)	7.916(-1)	6.160(-1)	2.749(-1)	5.351(-2)	1.065(-2)	1.519(-3)	8.818(-5)
20.....	7.160(-1)	6.900(-1)	5.360(-1)	2.359(-1)	4.416(-2)	8.769(-3)	1.254(-3)	7.558(-5)
21.....	3.500(-1)	3.415(-1)	2.863(-1)	1.360(-1)	2.500(-2)	4.983(-3)	7.151(-4)	3.796(-5)
22.....	4.973(-2)	4.877(-2)	4.296(-2)	2.110(-2)	4.958(-3)	9.245(-4)	1.745(-4)	8.377(-6)
23.....	1.310(-4)	1.293(-4)	1.160(-4)	6.346(-5)	1.822(-5)	6.842(-6)	3.622(-6)	3.572(-7)
$^{13}\text{CO}$ : Unattenuated Rate <sup>b</sup> $k_{10} = 2.034 \times 10^{-10} I_{\text{UV}} \text{ s}^{-1}$								
0.....	1.000	9.887(-1)	9.159(-1)	6.485(-1)	2.610(-1)	6.032(-2)	7.788(-3)	3.402(-4)
19.....	8.181(-1)	8.083(-1)	7.463(-1)	5.324(-1)	2.185(-1)	4.961(-2)	6.431(-3)	2.859(-4)
20.....	7.011(-1)	6.922(-1)	6.386(-1)	4.540(-1)	1.835(-1)	4.160(-2)	5.556(-3)	2.404(-4)
21.....	3.599(-1)	3.573(-1)	3.392(-1)	2.585(-1)	1.202(-1)	2.767(-2)	3.389(-3)	1.346(-4)
22.....	6.037(-2)	5.993(-2)	5.929(-2)	5.423(-2)	3.320(-2)	6.691(-3)	7.129(-4)	1.858(-5)
23.....	8.019(-4)	8.014(-4)	7.979(-4)	7.640(-4)	5.197(-4)	1.115(-4)	1.500(-5)	6.254(-7)
$\text{C}^{18}\text{O}$ : Unattenuated Rate <sup>b</sup> $k_{10} = 2.035 \times 10^{-10} I_{\text{UV}} \text{ s}^{-1}$								
0.....	1.000	9.897(-1)	9.243(-1)	6.673(-1)	2.921(-1)	9.464(-2)	1.451(-3)	7.450(-4)
19.....	8.088(-1)	8.000(-1)	7.450(-1)	5.405(-1)	2.383(-1)	7.686(-2)	1.194(-2)	6.310(-4)
20.....	7.032(-1)	6.953(-1)	6.477(-1)	4.708(-1)	2.091(-1)	6.811(-2)	1.042(-2)	5.071(-4)
21.....	3.611(-1)	3.587(-1)	3.424(-1)	2.655(-1)	1.371(-1)	4.805(-2)	6.614(-3)	2.436(-4)
22.....	6.093(-2)	6.059(-2)	6.005(-2)	5.592(-2)	4.069(-2)	1.480(-2)	1.640(-3)	3.276(-5)
23.....	9.061(-4)	9.061(-4)	9.042(-4)	8.855(-4)	7.410(-4)	2.968(-4)	3.616(-5)	8.619(-7)
$^{13}\text{C}^{18}\text{O}$ : Unattenuated Rate <sup>b</sup> $k_{10} = 2.043 \times 10^{-10} I_{\text{UV}} \text{ s}^{-1}$								
0.....	1.000	9.961(-1)	9.662(-1)	7.930(-1)	5.002(-1)	2.631(-1)	8.532(-2)	1.245(-2)
19.....	8.385(-1)	8.360(-1)	8.155(-1)	6.887(-1)	4.641(-1)	2.516(-1)	8.027(-2)	1.118(-2)
20.....	7.298(-1)	7.274(-1)	7.097(-1)	6.011(-1)	4.077(-1)	2.245(-1)	7.014(-2)	8.977(-3)
21.....	3.597(-1)	3.587(-1)	3.507(-1)	2.980(-1)	2.013(-1)	1.264(-1)	4.384(-2)	5.512(-3)
22.....	6.818(-2)	6.735(-2)	6.701(-2)	6.412(-2)	5.575(-2)	4.530(-2)	1.662(-2)	8.928(-4)
23.....	2.984(-3)	2.984(-3)	2.984(-3)	2.979(-3)	2.941(-3)	2.600(-3)	9.290(-4)	1.765(-5)

<sup>a</sup> These shielding functions have been computed for the unmodified Draine 1978 radiation field and the following parameters:  $b(\text{CO}) = 1.0 \text{ km s}^{-1}$ ,  $b(\text{H}_2) = 3.0 \text{ km s}^{-1}$ ,  $b(\text{H}) = 5.0 \text{ km s}^{-1}$ ,  $T_{\text{ex}}(\text{H}_2) = 10^{1.5} \text{ K}$ ,  $T_{\text{ex}}(\text{CO}) = 10 \text{ K}$ , and  $N(\text{H}) = 5 \times 10^{20} \text{ cm}^{-2}$ . The fixed abundance ratios of the isotopic varieties are  $^{12}\text{C}^{18}\text{O} : ^{13}\text{C}^{18}\text{O} : ^{12}\text{C}^{16}\text{O} = 1 : 1/45 : 1/500 : 1/2000$ . The shielding of the isotopic species is thus expressed as a function of the column density of  $^{12}\text{C}^{16}\text{O}$ .

<sup>b</sup> The unattenuated rate is the value that would apply for a cloud illuminated on one side only. For equal illumination of both sides of a finite slab, the boundary rate should be 1/2 times the listed unattenuated rate.



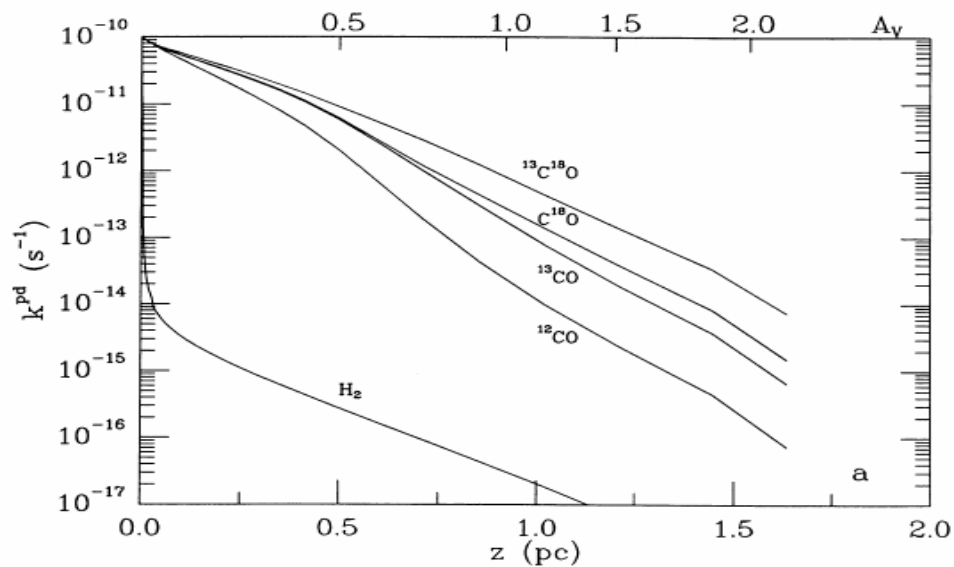


FIG. 5a

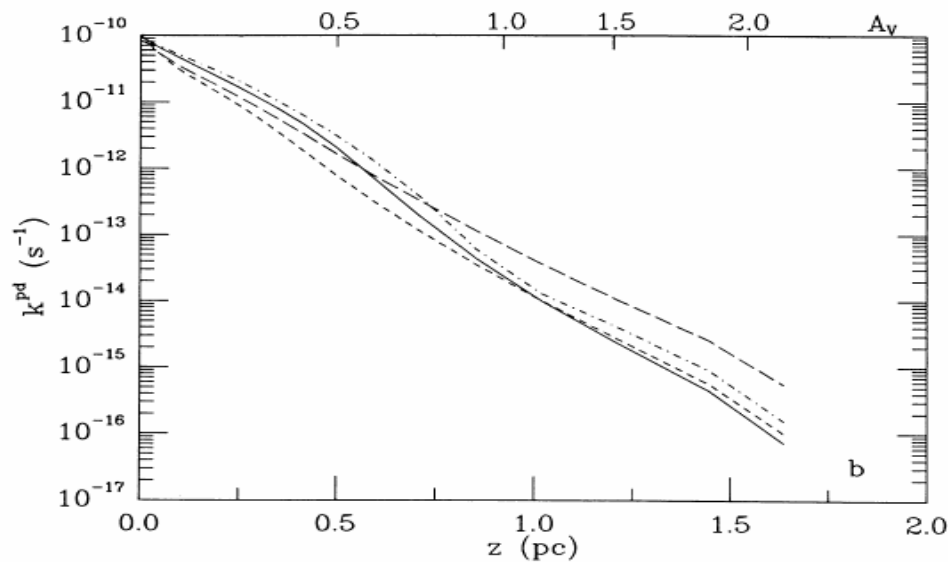


FIG. 5b

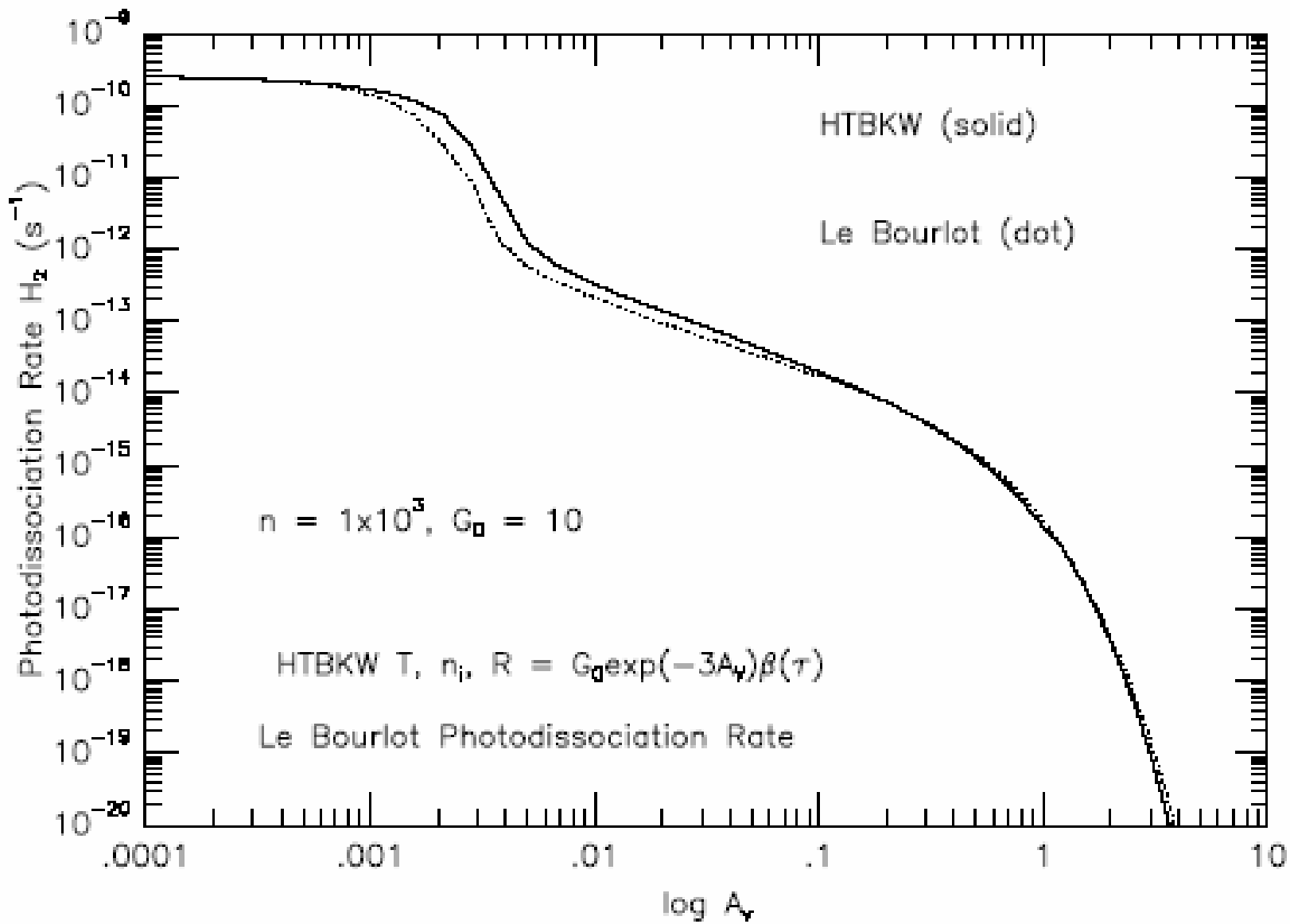
FIG. 5.—(a) Photodissociation rates of  $^{12}\text{CO}$  and the isotopic varieties as functions of linear depth into translucent cloud model T6. See Table 7 for details of the model. (b) Photodissociation rates of  $^{12}\text{CO}$  as functions of linear depth computed at four different levels of approximation. *Solid curve*: full calculation including self-shielding, mutual shielding, shielding by lines of H and  $\text{H}_2$  and dust attenuation for all CO lines up to  $J'' = 9$ . *Short-dashed curve*: calculation including only the  $R(0)$  lines of CO and  $\text{H}_2$  lines with  $J'' = 0$  and 1. *Long-dashed line*: calculation in which only self-shielding in the CO  $R(0)$  lines and dust attenuation is taken into account. *Dash-dotted line*: calculation using the shielding functions presented in Table 5.

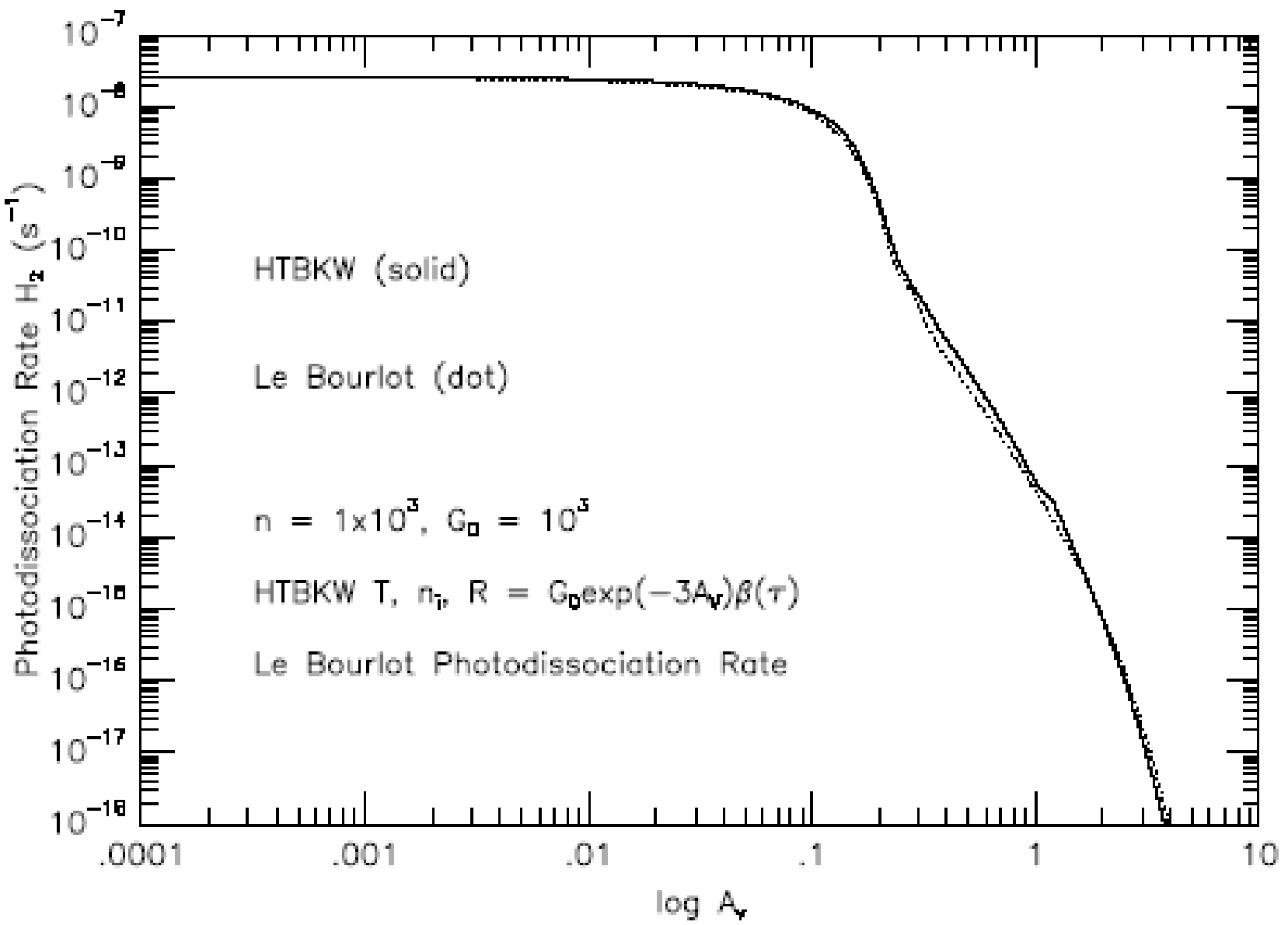
# Photorates with depth

- Good if line overlap is ignored; edge effects still occur;  $I_{\text{uv}}/n_{\text{H}}$  ratio crucial
- $\text{H}_2^*$  ( $\nu=6/2.6$  eV) versus  $\text{H}_2$  ( $J,\nu$ )
- Line overlap:  $\text{H}_2$ , H, CO, C
- MC  $\text{H}_2$ :  $N=135$ ,  $\lambda=1000$  Å,  $f=3.5(-3)$ ,  
 $A=5.7(8)$  s $^{-1}$ ,  $\eta=0.127$
- MC CO:  $N=33$ ,  $\lambda=1002$  Å,  $f=2.0(-2)$ ,  
 $A=3.0(11)$ ,  $\eta=1.0$

# Photorates with depth

- Should integrate photo-ionization and photo-dissociation cross sections:  $\sigma(\lambda)$
- Note: CRs and X-rays can be important; CRs no attenuation, X-rays column of  $N_H \sim 10^{22} \text{ cm}^{-2}$





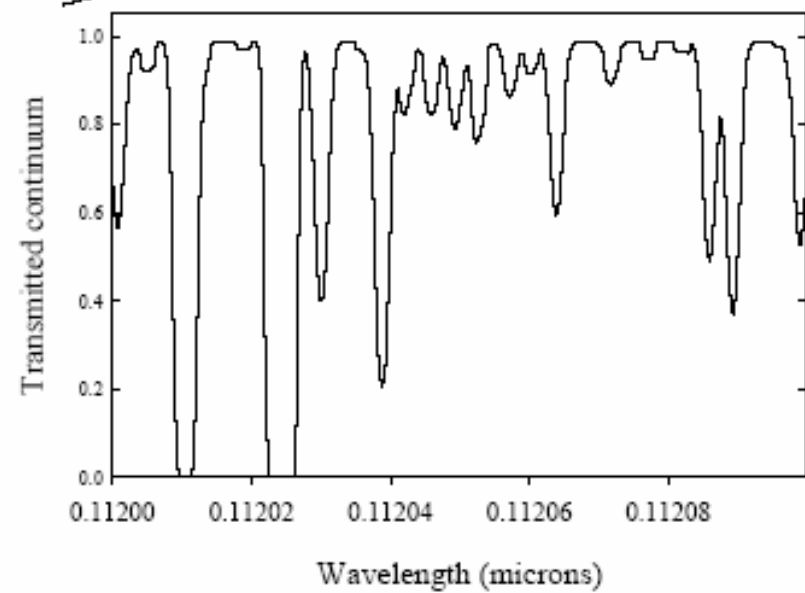
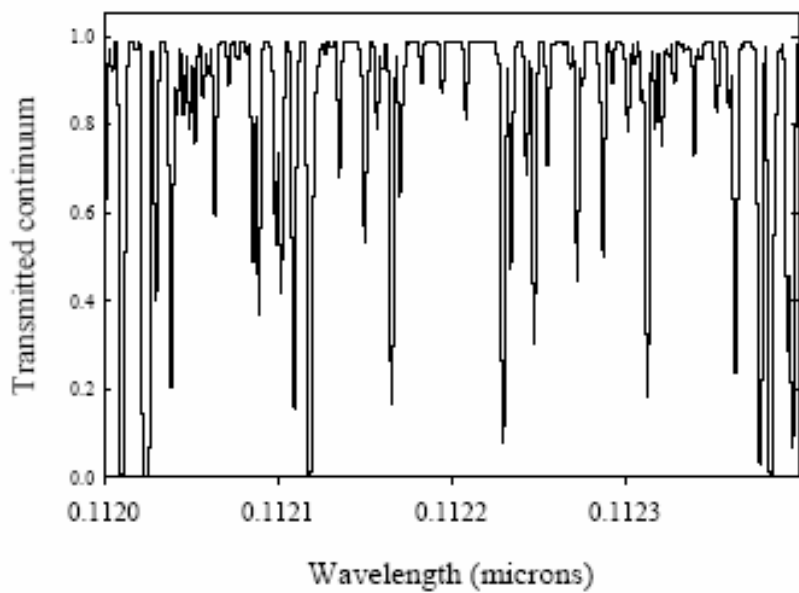
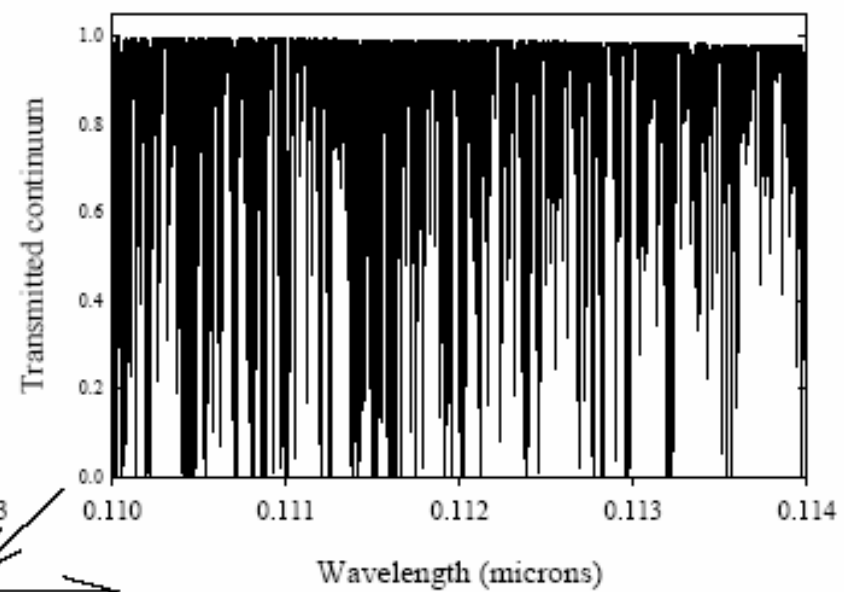
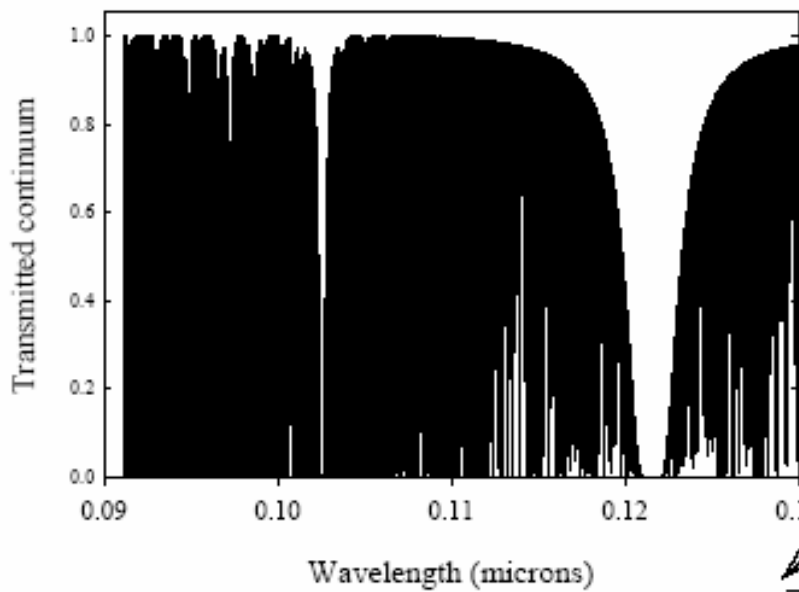


TABLE 2  
PHOTOIONIZATION AND DISSOCIATION RATES FOR DIFFERENT BLACKBODY RADIATION FIELDS WITH  $G_0 = 1$

Reaction	$T_{eff}$ in K															
	6000		8000		10,000		14,000		18,000		24,000		30,000			
	a	b	a	b	a	b	a	b	a	b	a	b	a	b		
C → C <sup>+</sup> + e <sup>-</sup>	2.82(-15)	3.27	2.70(-13)	3.30	3.50(-12)	3.33	4.92(-11)	3.36	1.63(-10)	3.38	3.42(-10)	3.39	4.50(-10)	3.40		
CH <sup>†</sup> → C + H <sup>+</sup>	3.86(-13)	1.35	1.17(-12)	1.41	3.24(-12)	1.59	2.12(-11)	2.02	6.90(-11)	2.31	1.62(-10)	2.57	2.36(-10)	2.71		
OH → O + H	6.66(-13)	1.81	7.70(-12)	1.90	3.12(-11)	1.94	1.28(-10)	2.00	2.30(-10)	2.05	3.00(-10)	2.10	3.08(-10)	2.14		
CH → C + H	8.30(-11)	1.32	2.10(-10)	1.37	3.60(-10)	1.43	6.62(-10)	1.56	8.32(-10)	1.65	8.20(-10)	1.74	7.18(-10)	1.78		
CH → CH <sup>+</sup> + e <sup>-</sup>	8.12(-15)	3.10	7.08(-13)	3.16	8.80(-12)	3.20	1.19(-10)	3.25	3.88(-10)	3.28	8.02(-10)	3.39	1.05(-9)	3.32		
H <sub>2</sub> O → OH + H	1.65(-12)	1.84	1.92(-11)	1.86	7.28(-11)	1.89	2.76(-10)	1.94	4.78(-10)	1.99	6.14(-10)	2.05	6.30(-10)	2.10		
CH <sub>2</sub> → CH + H	1.15(-11)	2.00	8.78(-11)	1.99	2.50(-10)	1.98	6.42(-10)	1.98	8.56(-10)	1.98	8.42(-10)	2.00	7.32(-10)	2.01		
Mg → Mg <sup>+</sup> + e <sup>-</sup>	1.66(-11)	1.95	2.48(-12)	1.96	1.05(-11)	1.98	4.16(-11)	2.00	7.92(-11)	2.01	8.06(-11)	2.03	7.58(-11)	2.04		
SiO → Si + O	1.62(-13)	2.17	3.62(-12)	2.18	1.94(-11)	2.19	9.90(-11)	2.21	1.87(-10)	2.22	2.42(-10)	2.23	2.40(-10)	2.24		
Fe → Fe <sup>+</sup> + e <sup>-</sup>	2.12(-13)	2.08	4.30(-12)	2.12	2.24(-11)	2.14	1.13(-10)	2.17	2.12(-10)	2.19	2.74(-10)	2.21	2.72(-10)	2.22		
S → S <sup>+</sup> + e <sup>-</sup>	1.20(-14)	2.78	7.50(-13)	2.84	7.64(-12)	2.89	9.10(-11)	2.95	2.80(-10)	3.00	5.58(-10)	3.05	7.20(-10)	3.07		
O <sub>2</sub> → O + O	1.13(-12)	1.98	1.86(-11)	2.01	8.46(-11)	2.03	3.64(-10)	2.06	6.40(-10)	2.08	7.88(-10)	2.10	7.72(-10)	2.12		
Si → Si <sup>+</sup> + e <sup>-</sup>	1.77(-12)	2.13	3.80(-11)	2.15	2.40(-10)	2.17	1.07(-9)	2.21	2.10(-9)	2.23	2.84(-9)	2.26	2.92(-9)	2.27		
H <sub>2</sub> <sup>†</sup> → H + H <sup>+</sup>	3.78(-13)	1.95	5.40(-12)	2.01	2.84(-11)	2.07	1.49(-10)	2.16	3.08(-10)	2.22	4.48(-10)	2.28	4.88(-10)	2.32		
H <sub>2</sub> → H + H	2.02(-17)	2.50	2.72(-15)	2.50	4.48(-14)	2.50	9.25(-13)	2.50	4.55(-12)	2.50	1.68(-11)	2.50	3.41(-11)	2.50		
CO → C + O	9.20(-17)	3.20	1.05(-14)	3.20	1.62(-13)	3.20	3.39(-12)	3.20	1.74(-11)	3.20	7.16(-11)	3.20	1.60(-10)	3.20		

NOTES.—The reaction rates are parameterized by  $a$  and  $b$  according to  $R = a \times e^{-b\lambda r}$ , where  $a$  is the unattenuated rate. The exponent  $b$  reflects only the attenuation due to dust, but not that due to self-shielding or shielding by H<sub>2</sub>.

† Notice that this reaction differs from the one given in TH85, Table 5, p.742.

# References

- Tielens & Hollenbach 1985
- Kaufman et al. 1999; Spaans 1996; Sternberg & Dalgarno 1995; Störzer et al. 1995; Spaans et al. 1994; Wolfire et al. 1993; le Bourlot et al. 1993; Tielens et al. 1993; Boisse' 1990; van Dishoeck & Black 1988; Sternberg 1988; Black & van Dishoeck 1987; de Jong et al. 1980; Black & Dalgarno 1976
- Maloney et al. 1996